

Factor Completely:

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| <p>1) <math>9x^2 + 42x - 15</math><br/> <math>3(3x^2 + 14x - 5)</math><br/> <math>3(3x-1)(x+5)</math></p> <div style="text-align: center;"> <math display="block">\begin{array}{r} \text{a.c} \\ -15 \\ \hline 15 \quad -1 \\ \hline 14 \\ \hline b \\ \hline \frac{15}{3} \quad \frac{-1}{3} \end{array}</math> </div> | <p>2) <math>x^3 - 3x^2 - 9x + 27</math><br/> <math>x^2(x-3) - 9(x-3)</math><br/> <math>(x-3)(x^2-9)</math><br/> <math>(x-3)(x-3)(x+3)</math><br/> or <math>(x+3)(x-3)^2</math></p> |
| <p>3) <math>4x^2 - 100</math><br/> <math>4(x^2 - 25)</math><br/> <math>4(x+5)(x-5)</math></p>   | <p>4) <math>x^4 + 27x</math><br/> <math>x(x^3 + 27)</math> Sum of Cubes <math>a^3 + b^3</math><br/> <math>(a+b)(a^2 - ab + b^2)</math><br/> <math>x(x+3)(x^2 - 3x + 9)</math></p>  |

Simplify the complex expressions.

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| <p>5) <math>(10-2i) + (-3-24i)</math><br/> <math>10 + -3 = 7</math><br/> <math>-2i + -24i = -26i</math><br/> <math>7 - 26i</math></p> | <p>6) <math>(-3+i)(5-7i)</math> Dist. Property<br/> <math>-15 + 21i + 5i - 7i^2 \leftarrow i^2 = -1</math><br/> <math>-15 + 21i + 5i + 7</math><br/> <math>-8 + 26i</math></p> | <p>7) <math>6i(-10+3i)</math> Dist. Prop.<br/> <math>-60i + 18i^2 \leftarrow i^2 = -1</math><br/> <math>-18 - 60i</math></p> |
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Rationalize the denominator.

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| <p>8) <math>\frac{2\sqrt{5}}{\sqrt{7}} \cdot \frac{\sqrt{7}}{\sqrt{7}} = \frac{2\sqrt{35}}{7}</math></p> | <p>9) <math>\frac{3}{2i} \cdot \frac{-2i}{-2i} \left\{ \frac{3}{0+2i} \cdot \frac{0-2i}{0-2i} \right.</math><br/> <math>\rightarrow \frac{-6i}{-4i^2} = \frac{-6i}{4} = \frac{-3i}{2}</math></p> | <p>10) <math>\frac{-7}{3-4i} \cdot \frac{3+4i}{3+4i} = \frac{-21-28i}{9+12i-12i-16i^2}</math><br/> <math>\frac{-21-28i}{25}</math> or <math>\frac{-21}{25} - \frac{28}{25}i</math></p> |
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Solve for each.

11)  $4(3x-5)(x+4)=0$

$$3x-5=0 \text{ or } x+4=0$$

$$x = \frac{5}{3} \text{ or } x = -4$$

12) Solve:  $\frac{1}{3}(x+2)^2 - 14 = 0$

$$\frac{1}{3}(x+2)^2 = 14$$

$$(x+2)^2 = 42$$

$$x+2 = \pm\sqrt{42}$$

$$x = -2 \pm \sqrt{42}$$

13)  $-3x^2 + 33x - 81 = 0$  Divide by  $-3$

$$x^2 - 11x + 27 = 0$$

$$x = \frac{-(-11) \pm \sqrt{(-11)^2 - 4(1)(27)}}{2(1)} = \frac{11 \pm \sqrt{13}}{2}$$

14)  $4x^2 - 3x - 19 = 23 + x - 2x^2$

$$6x^2 - 4x - 42 = 0 \text{ Divide by } 2$$

$$3x^2 - 2x - 21 = 0$$

$$(3x+7)(x-3) = 0$$

$$x = -\frac{7}{3} \text{ or } x = 3$$

$$\begin{array}{r} -63 \\ 7 \times -9 \\ -21 \\ \hline -9 \\ 7 \\ \hline -9 \\ 7 \end{array}$$

15)  $-4(x+3)^2 - 24 = 0$

$$-4(x+3)^2 = 24$$

$$(x+3)^2 = -6$$

$$x+3 = \pm\sqrt{6}i$$

$$x = -3 \pm \sqrt{6}i$$

16)  $2x^2 + 21 = 111$

$$2x^2 = 90$$

$$x^2 = 45$$

$$x = \pm\sqrt{45} = \pm\sqrt{9}\sqrt{5}$$

$$x = \pm 3\sqrt{5}$$